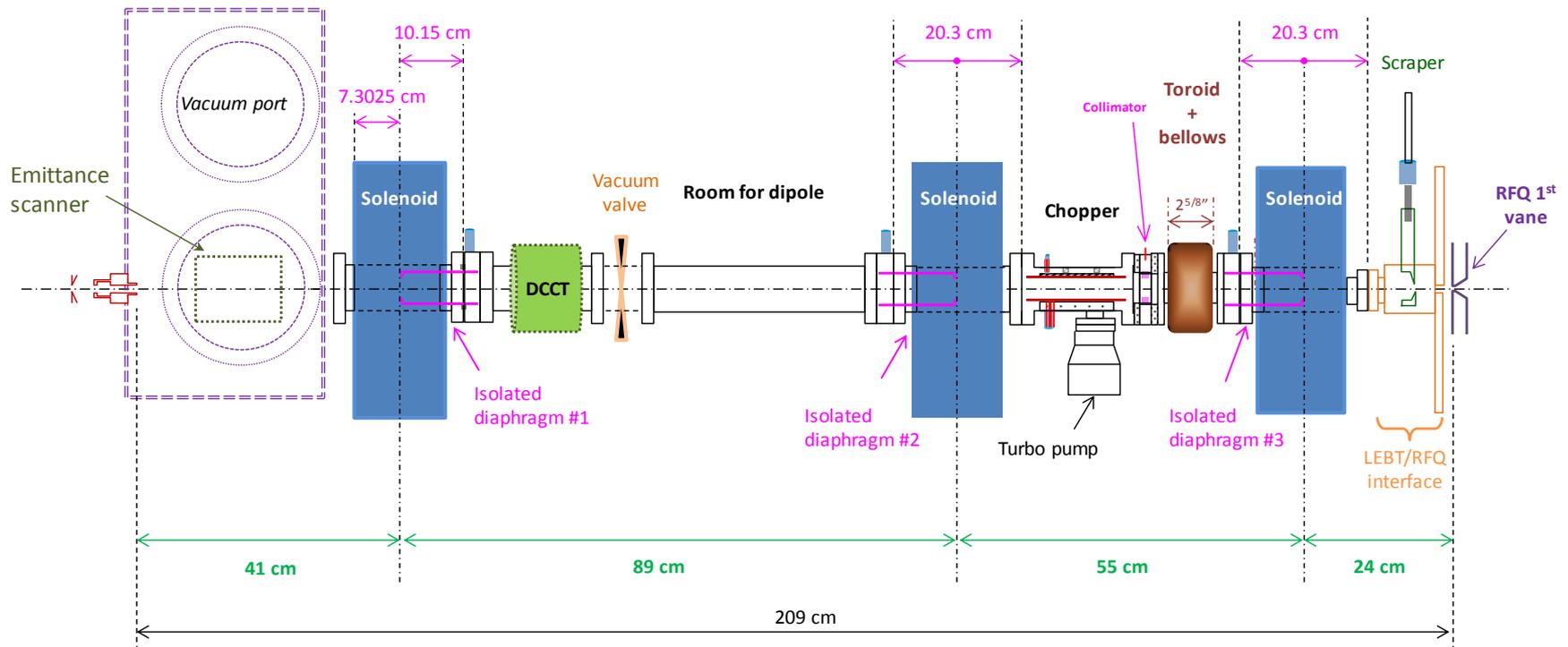


# **Peculiarities of the emittance growth in LEBT**

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January 21, 2014



- H<sup>-</sup>, 30 keV, up to 10 mA DC
- Capability to create 1 $\mu$ s – 16 ms pulses at 60 Hz with the chopper
- Isolated diaphragms for stopping the residual gas ions
- Possibility to test a concept of partially neutralized transport



- Simulations showed that even at modest currents of PXIE LEBT, the space charge can significantly increase the emittance

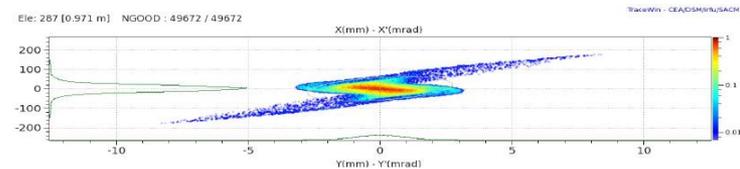
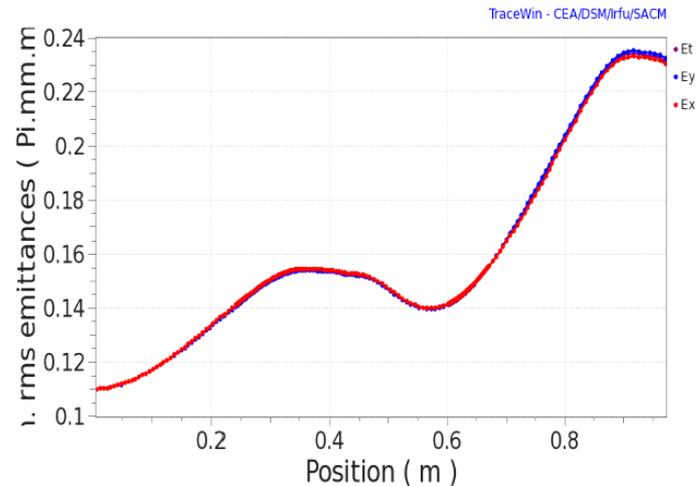
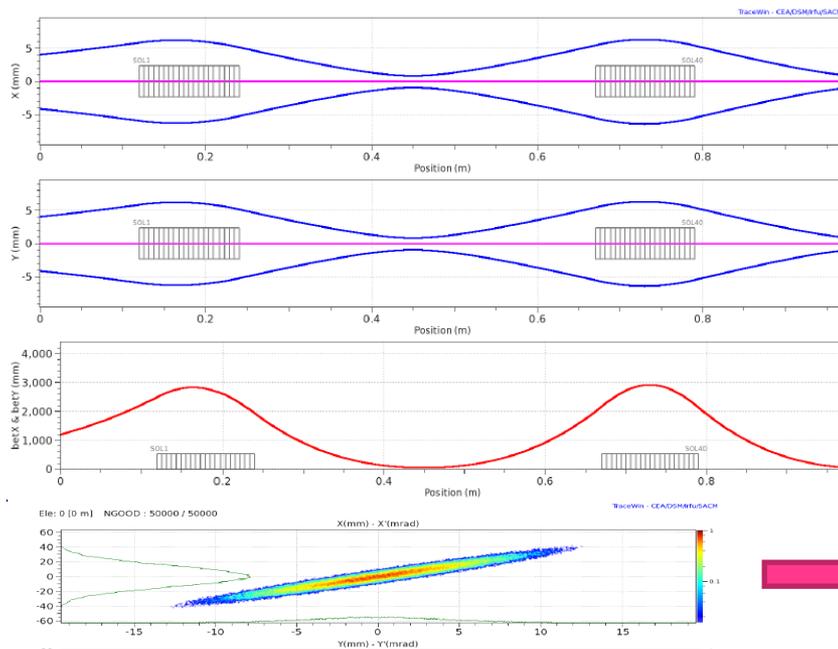
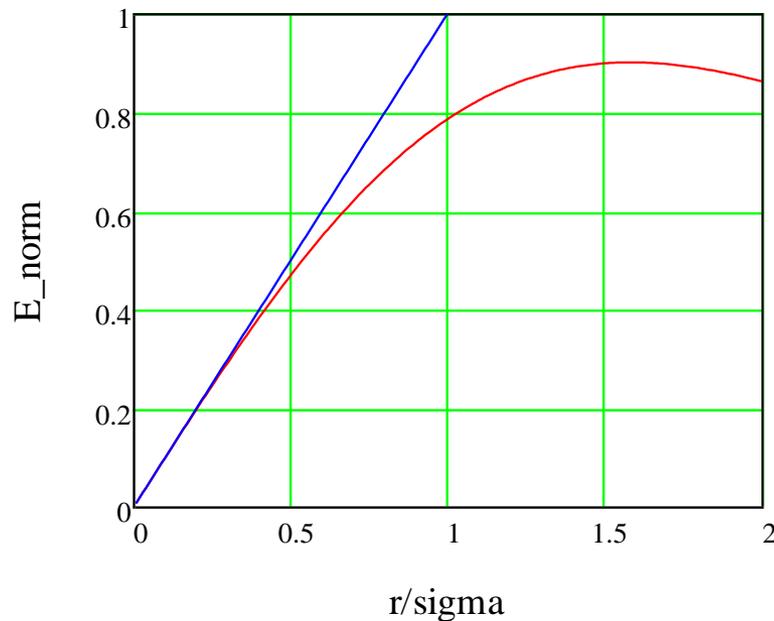


Illustration: 2 – solenoid LEBT, H-, 30 keV, 5 mA, initial beam is Gaussian in space and transverse momentum. No neutralization.

Simulation by TraceWin. J.-F Ostiguy & N. Solyak, Apr 2, 2012.



- The dominant source of the emittance growth is non – linear forces from the beam space charge



Example:  
Electric field of a beam with  
Gaussian density distribution of  
density (red). Blue – a straight  
line for comparison.

- How can one decrease this growth?



- Standard answer in LEBTs: space charge neutralization by ions of the residual gas
  - No space charge => no non-linear forces => no related emittance growth
  - However, having no neutralization at the LEBT chopper and downstream would be beneficial to avoid variations during transition from pulse regime to DC regime
    - Presently, all PXIE commissioning is assumed to be made with a pulsed beam of  $\sim 5 \mu\text{s}$  width.

16 KeV, 3 mA H- Beam pulsed @ 50% duty factor

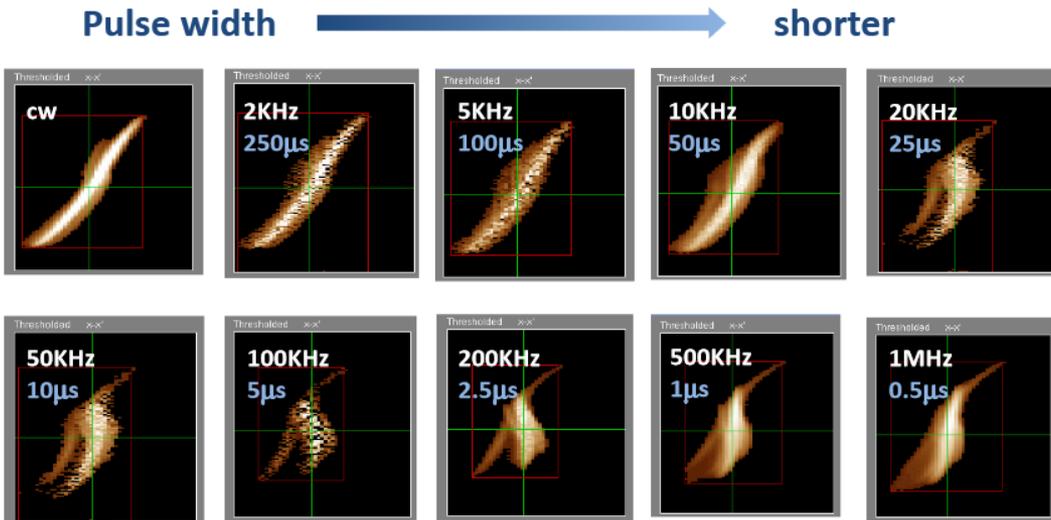


Illustration: phase portraits of an H<sup>-</sup> beam at different pulse durations.  
 Qing Ji (LBNL), PXIE ion source.  
 PX meeting, November 27, 2012.



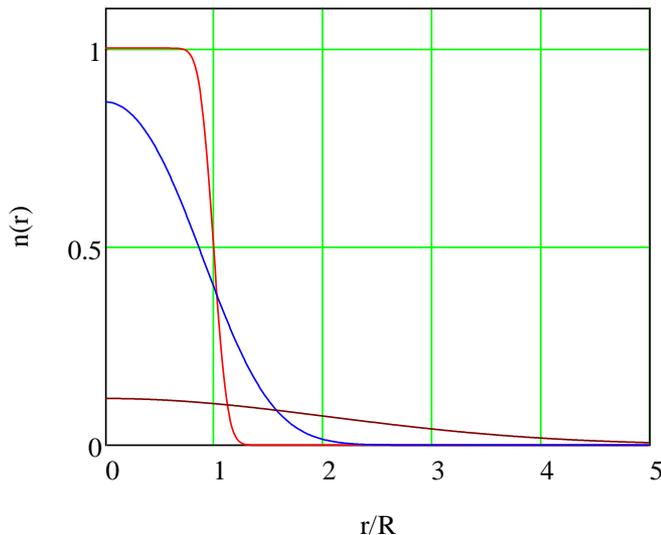
- The emittance doesn't grow if the current density distribution is constant
  - The space charge force is linear with radius
- The distribution may stay close to constant if the beam transport is space charge – dominated
  - Cannot be fulfilled everywhere in the LEBT
    - Requires strong focusing
    - Pressure is high near the ion source ( $>1.E-5$  Torr), thus neutralization is unavoidable



- Let's consider a zero-current beam with initially constant current density but a Gaussian transverse velocity distribution

$$\frac{\partial^2 n}{\partial V_x \partial V_y} = \frac{1}{2\pi\sigma_V^2} \exp\left(-\frac{V_x^2 + V_y^2}{2\sigma_V^2}\right) \cdot \begin{cases} 1, & r \leq R \\ 0, & r > R \end{cases}$$

- When the beam expands, a particle position is determined mainly by its initial transverse velocity rather than initial position, and the current density approaches a Gaussian shape



Evolution of the density profile of a beam with initially constant current density and a Gaussian distribution of transverse velocities after traveling a distance  $L$  with the longitudinal velocity  $V_z$ .

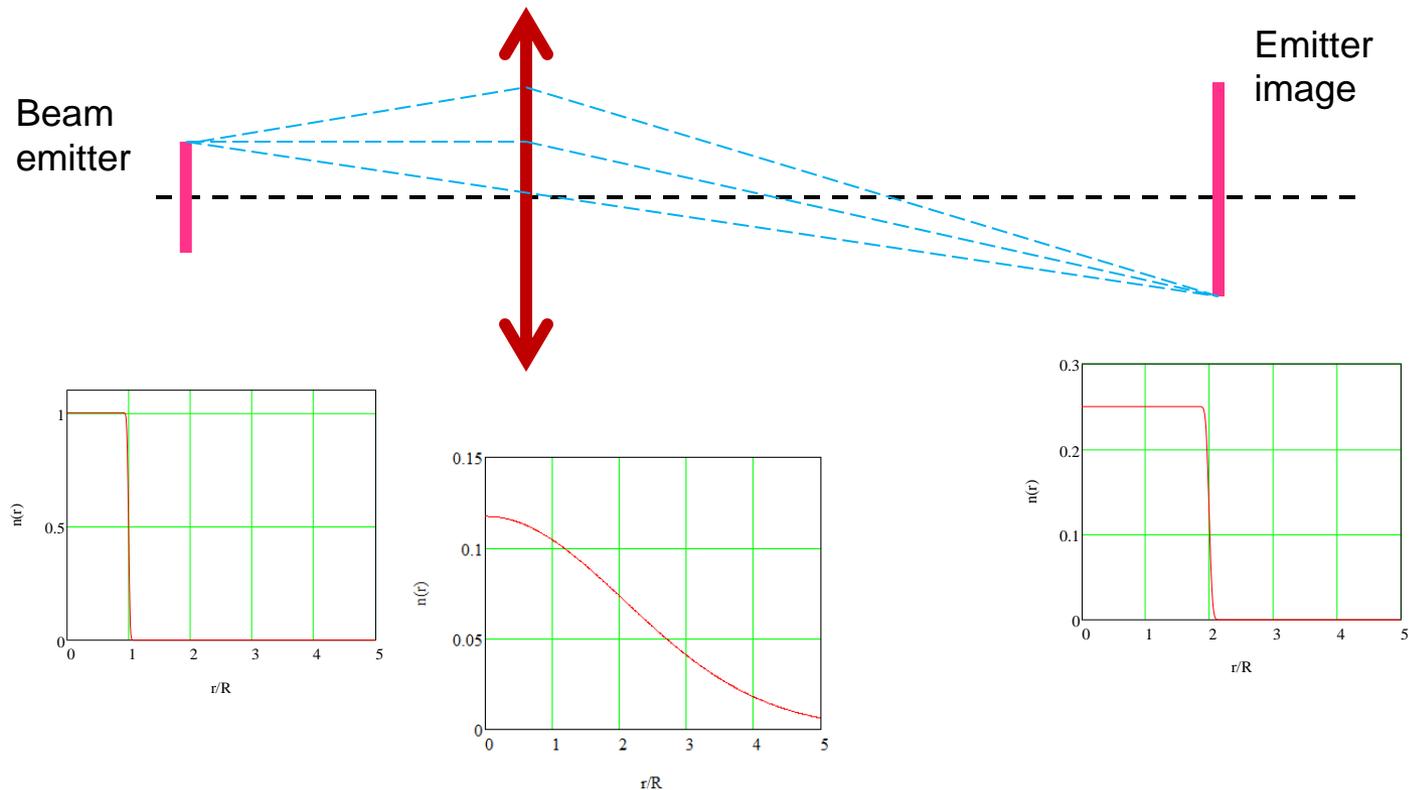
Parameter  $\sigma = \frac{L}{R} \cdot \frac{\sigma_V}{V_z}$  characterizes

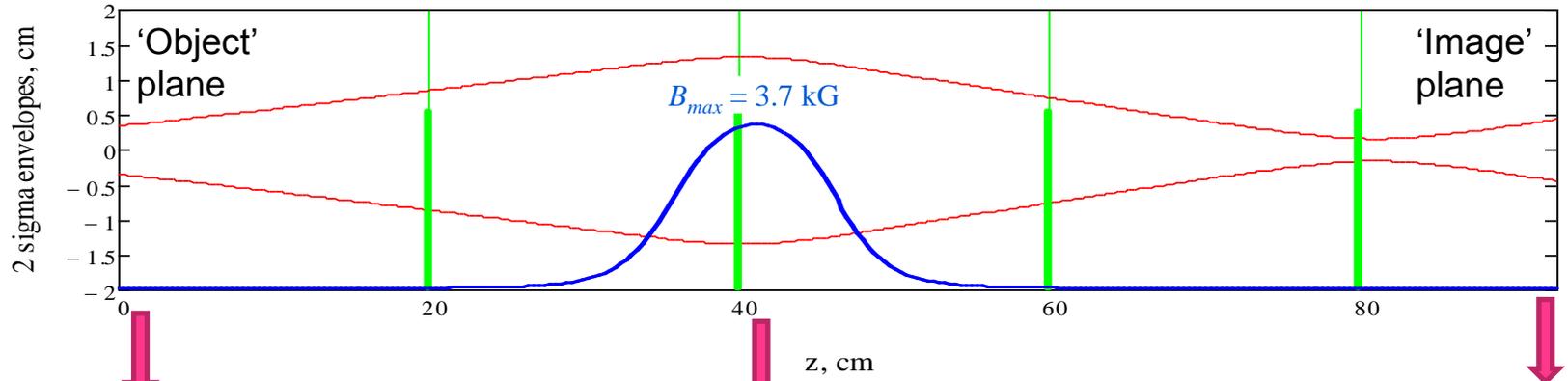
the relative increase of the beam size.

The value of  $\sigma$  is for the **red curve 0.1**, **blue – 0.5**, **brown – 2**.

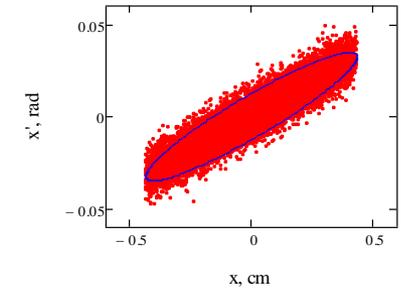
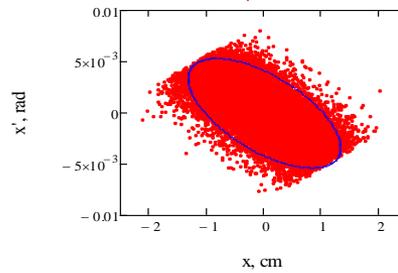
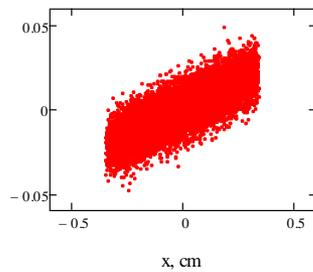


- Focusing with an ideal lens reproduces the constant density distribution at the image plane

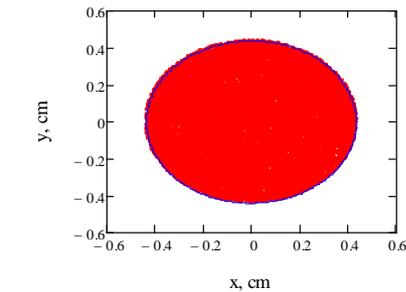
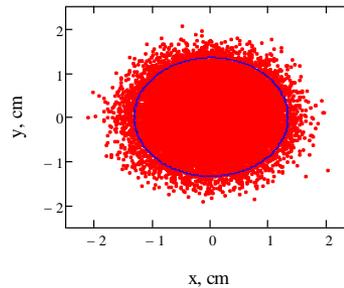
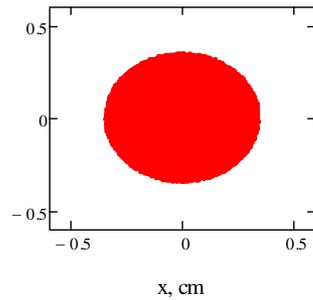




X-X'



X-Y

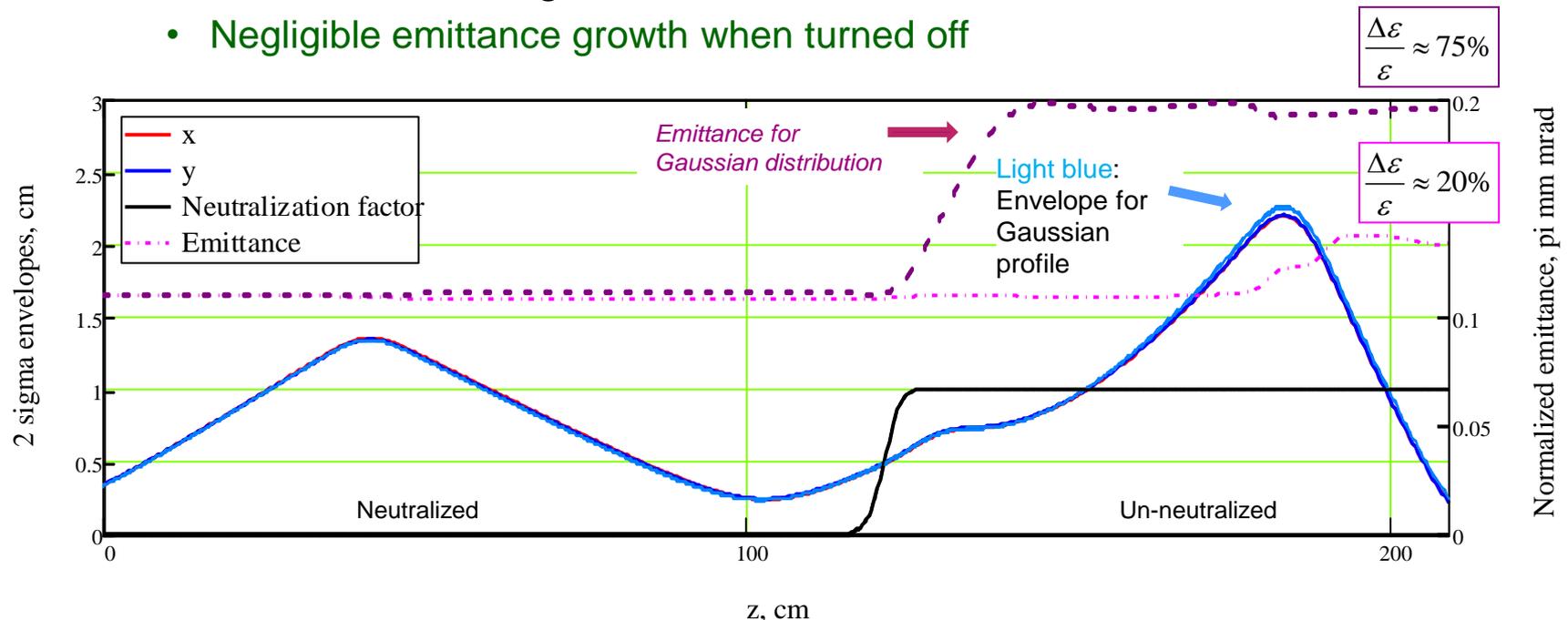




- Recipe to combine a small emittance growth, neutralization near the ion source, and un-neutralized transport through a downstream portion of the LEBT
  - Create in the ion source a beam with a constant density distribution
  - Let it expand in the neutralized area
    - Emittance doesn't grow because the space charge is turned off
  - Focus with a low-aberration lens to get an image spot with the size preferably larger than the emitter's
  - Interrupt neutralization
  - Make the un-neutralized section as short as possible
    - Emittance growth is low because the distribution is close to constant

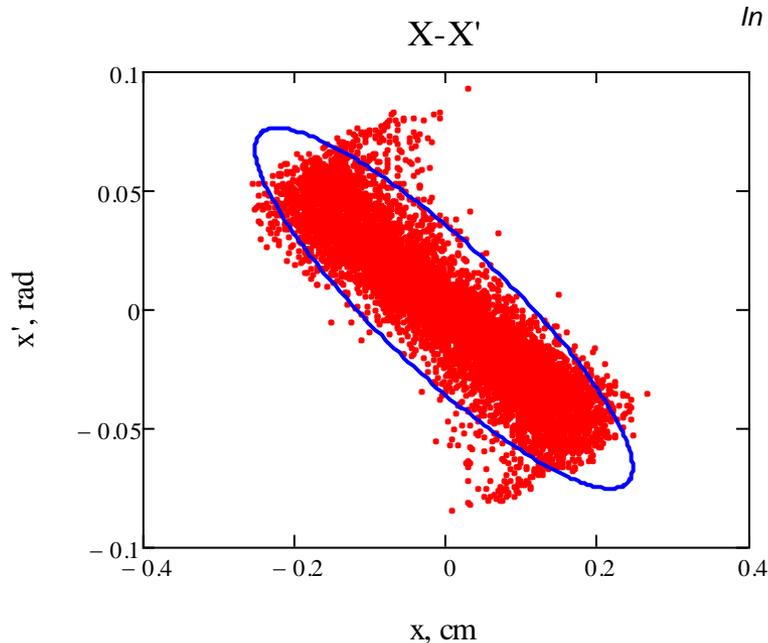


- Dynamics of the beam with initial constant current density in the PXIE LEBT was simulated with Valery's MathCad code
  - Emittance growth is significantly lower than in a case of a double-Gaussian distribution:  $\sim 20\%$  vs.  $\sim 75\%$  (for similar envelope profiles)
  - Source of emittance growth: solenoid aberrations
    - Negligible emittance growth when turned off



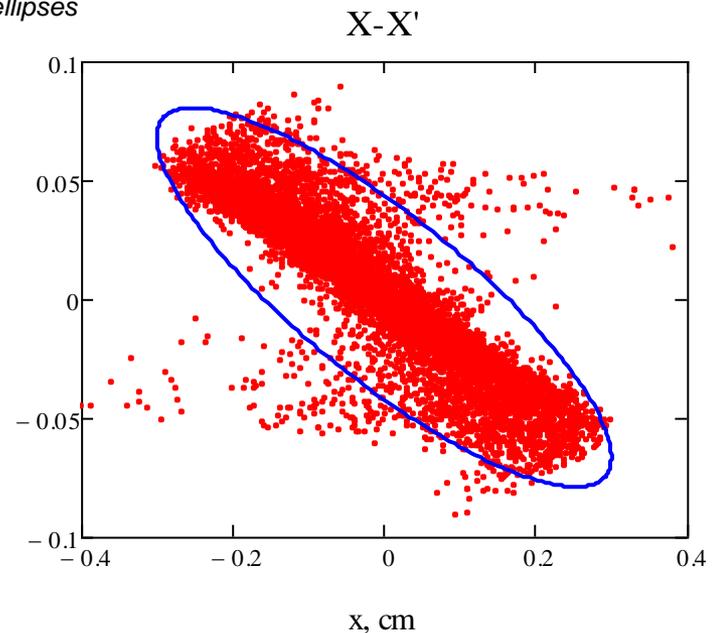


- Phase space portraits at the exit of the LEBT corresponding to the beam envelopes shown on the previous slide
  - 7500 macro-particles



Uniform current density distribution  
(Gaussian distribution for velocities)

In blue: 4 rms ellipses

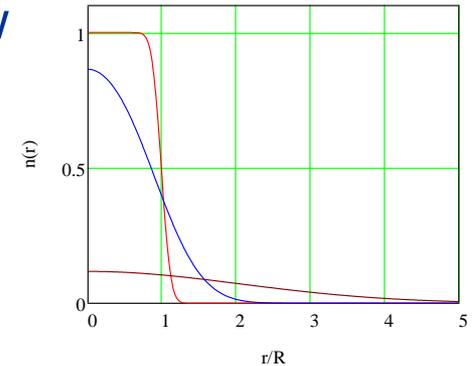


Gaussian current density distribution  
(Gaussian distribution for velocities)

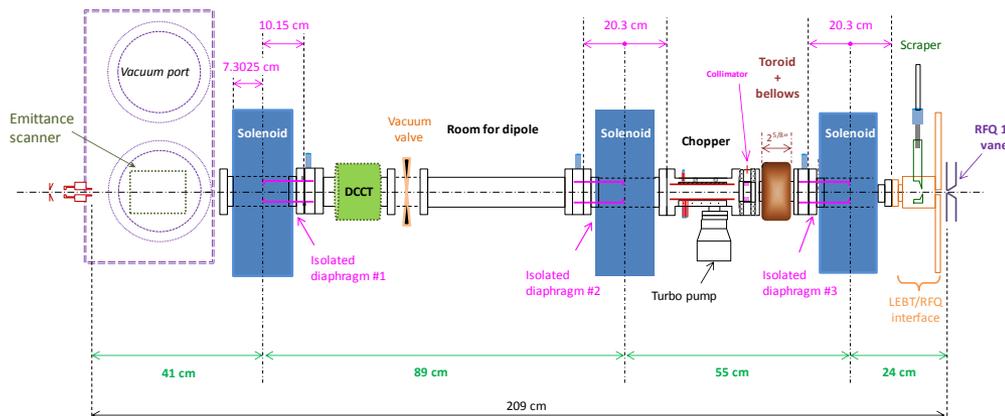


- The length of the un-neutralized section with low disturbance grows with the beam radius at the transition

- Parameter  $\sigma$  determines the distribution shape
- For a fixed  $\sigma$ ,
 
$$L = \frac{R}{\sigma} \cdot \frac{V_z}{\sigma_V} = \frac{1}{\sigma} \cdot \frac{1}{\epsilon} \cdot R^2$$

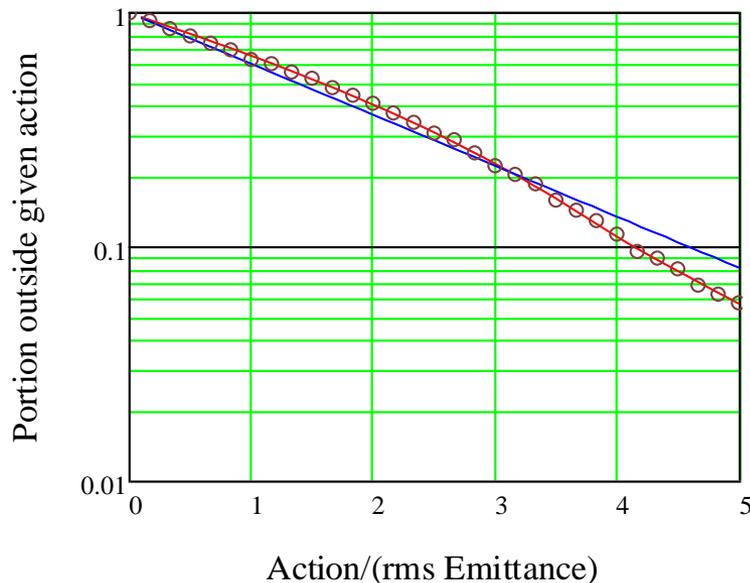


- The maximum diameter of the beam waist is determined by parameters of the chopping system: available space and the kicking voltage





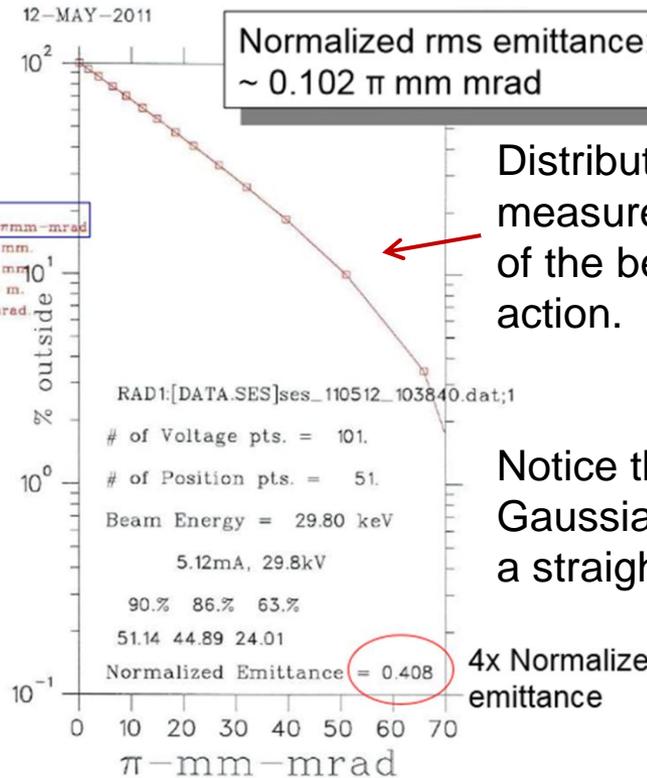
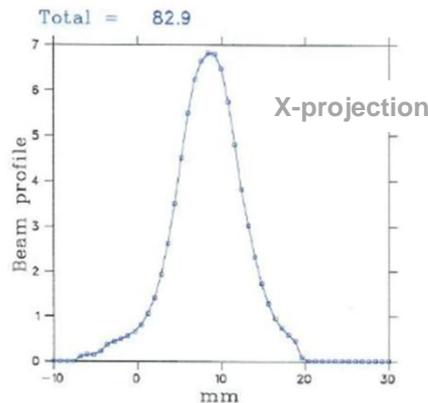
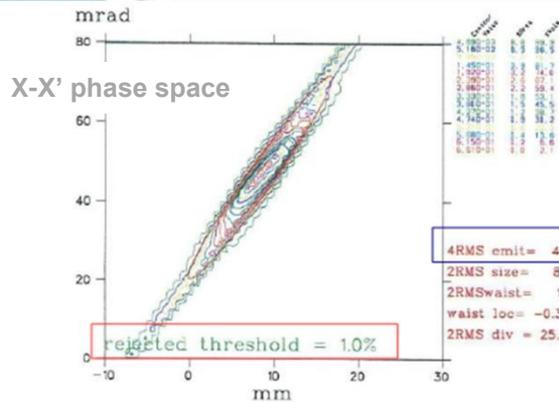
- Typical assumption in simulations: Gaussian distribution both in space and velocity (“double-Gaussian”)
- How close is this assumption to reality?
  - Can look at the measurements of the PXIE ion source made during the acceptance tests
  - Need to look at deviations from the double-Gaussian



Portion of particles outside of a given action. **Blue** – double-Gaussian (a straight line in semi-logarithmic scale). **Red** – constant current density. **Circles** – experimental data (see the next slide).



## Emittance Measurement – 5mA, 30keV

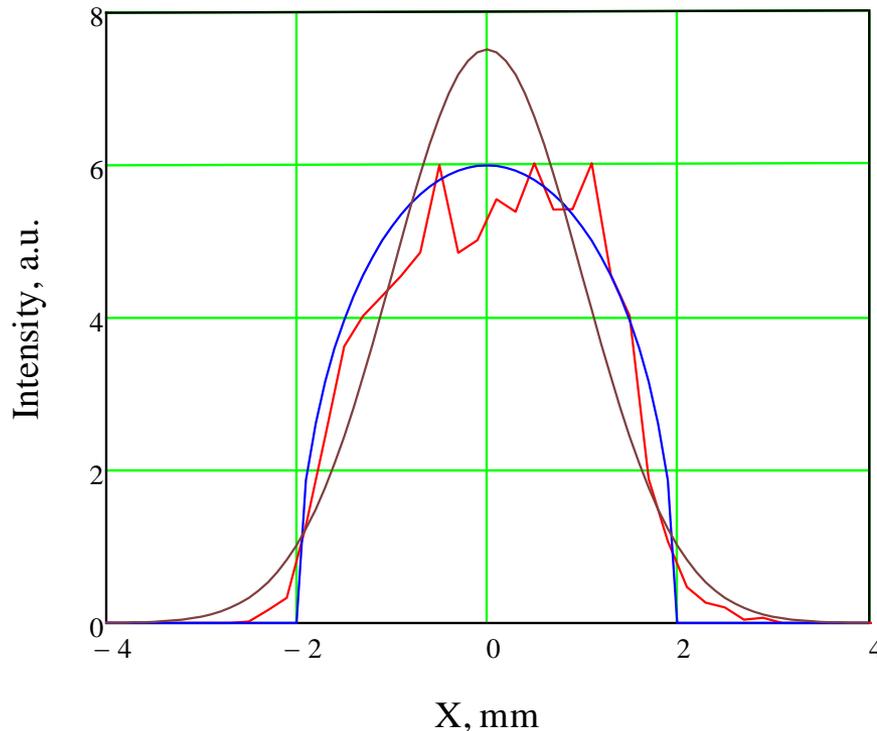


Distribution in PXIE source as measured at TRIUMF: portion of the beam outside of a given action.

Notice that it is not exactly Gaussian distribution (i.e. not a straight line).



- One can propagate the measured distribution back to the minimum size (vertical phase-space trace ellipse) and look at the X–projection
  - The thus-obtained distribution is closer to the one resulting from a constant-density distribution than to a Gaussian



**Red** – projection of the measured distribution to X after back propagation in free space. **Blue/Brown**– X-projections for beam with a **constant density/Gaussian profile** and the same second moments and integrals.



- 
- Phase space distribution in PXIE ion source is likely closer to (constant in space)\*(Gaussian in velocities) than to double-Gaussian
  - A scheme with expanding the beam size in a neutralized space and interrupting the neutralization where the beam spatial distribution is nearly constant allows suppressing the space charge-related emittance growth
  - Measurements in FY14 at the PXIE LEBT can be used to test such a scheme